Pre-College Math

Unit 4 Notes

#### 4.1 Solving Systems of Linear Equations by Graphing

### **EXAMPLE 1** Determining Whether an Ordered Pair Is a Solution

Decide whether the ordered pair (4, -3) is a solution of each equation. (a) x + 4y = -8 (b) 2x + 5y = -7

(a) 
$$x + 4y = -8$$

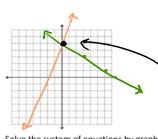
**(b)** 
$$2x + 5y = -7$$

yes (4,-3) is a solution

yes solution

# EXAMPLE 2 Solving a System by Graphing

Solve the system of equations by graphing both equations on the same axes.



$$y = \frac{-2}{3}x + 5 \qquad \begin{cases} m = -\frac{2}{3} \\ 6 = 5 \end{cases}$$

$$y = 3x + 5$$
  $M = 3$ 

Solution is the point of intersection

(0, 5)

Solve the system of equations by graphing.

$$y = \frac{1}{2}x - 3$$
  $m = \frac{1}{2}$ 

$$y = 3x - 3$$

$$y = \frac{1}{2}x + 1$$
  $m = \frac{1}{2}$ 









## **EXAMPLE 3** Solving Special Systems by Graphing

Solve each system by graphing.

(a) 
$$y = -2x + 2$$

y = -2x + 8

$$y = \frac{-2}{5}x + 2$$
  $x = -\frac{2}{5}$   $x = 2$ 

$$6x + 15y = 30$$



$$\frac{5y}{15} = \frac{-6x}{15} + \frac{30}{15}$$

$$y = -\frac{6x}{15} + 2 \\ y = -\frac{2x}{5} + 2$$

Three cases for solutions of systems

one solution

No Solution \ I ms

parallel lines \ Same lune

Classification:

### **EXAMPLE 4** Identifying the Three Cases by Using Slopes

Describe each system without graphing. State the number of solutions.

(a) 
$$3x + 2y = 6$$
  
 $-2y = 3x - 5$ 

**(b)** 
$$2x - y = 4$$

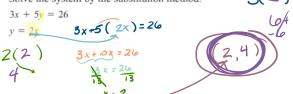
$$x = \frac{y}{2} + 2$$

(c) 
$$x - 3y = 5$$
  
 $2x + y = 8$ 

### 4.2 Solving Systems of Linear Equations by Substitution

### EXAMPLE 1 Using the Substitution Method

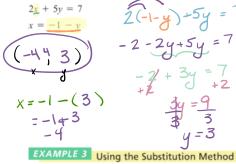
Solve the system by the substitution method.





### **EXAMPLE 2** Using the Substitution Method

Solve the system by the substitution method.



Use substitution to solve the system.

$$y = 4 - 2x$$
$$5x + 3y = 10$$

### **EXAMPLE 4** Solving an Inconsistent System by Substitution

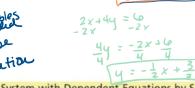
Use substitution to solve the system.

$$x = 5 - 2v$$
$$2x + 4y = 6$$



Same

-4y +4y = 6 -10 -4y +4y = 6 -4y +4y = -4 -4y +4y = -4 conclus False



EXAMPLE 5 Solving a System with Dependent Equations by Substitution

Solve the system by the substitution method.

$$\frac{-y}{-9x} = \frac{4 - 3x}{3y} = \frac{-4 + 3x}{-12}$$

$$-9x + 3y = -12$$

$$-9x - 12 + 9x = -12$$

$$-12 = -12$$

$$-12 = -12$$

$$-13x = -12$$

$$-12 = -12$$

$$-13x = -12$$

# EXAMPLE 6 Using the Substitution Method with Fractions as Coefficients

Solve the system by the substitution method.

Solve the system by the substitution 
$$\begin{array}{c}
12x + y = 8 \\
2x + 3y = -10
\end{array}$$

$$\begin{array}{c}
12x + y = 8 \\
-2x + 3y = -12x + 8
\end{array}$$

#### 4.3 Solving Systems of Linear Equations by Elimination



Panera Bread is known for their delicious bagels, a popular choice for breakfast or a mid-afternoon snack. It's also a beloved item to bring to work. Peyton, Kelly, Carter, and Cecily take turns bringing food for their department each Friday.

1. Peyton's Panera Bread order is shown below. What is a possible cost for a single bagel and what is a possible cost for one tub of cream cheese? Explain your thinking 2.20 (8) = 17.60



\$19.50 (1) = 1.90 Cream \$19.95 19.50 West

2. Kelly bought 12 Cinnamon Crunch bagels and 3 tubs of plain cream cheese. If Panera charges fairly, how much should Kelly's order cost? How do you know? \$31.05

Tax 110.75

What do you think it means to charge fairly?

\$29.70 \$31,50

- 3. Assuming that Panera charges fairly, find the cost of a single bagel and a single tub of plain cream cheese or explain why this is not possible.
- 4. Carter loves Panera, so when it was his turn to bring food he ordered more Cinnamon Crunch bagels than Peyton and double the amount of cream cheese. His order is shown.
  - a) How does Carter's subtotal compare to Peyton's?



2.20 (13) = 28.60 1.90 (4) = 7.60  $35.25 \qquad 36.20$ 

b) Can you figure out the cost of a single bagel and the cost of a single tub of cream cheese?



Total

5. Cecily went to Panera and bought 7 bagels, 1 tub of cream cheese, and a salad. Her subtotal (before tax) was \$23.71. Find the cost of her salad.

\$35.44

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# EXAMPLE 1 Using the Elimination Method

Use the elimination method to solve the system.

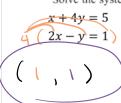
$$\begin{vmatrix} 1x + y = 5 \\ 1x - y = 3 \end{vmatrix}$$

$$\frac{2x}{2} = \frac{8}{2}$$

x = 4

### **EXAMPLE 2** Using the Elimination Method

Solve the system.



$$1x + 4y = 5$$
  
 $+ 8x - 4y = 4$   
 $9x = 9$   
 $x = 1$   
 $x = 1$ 

## EXAMPLE 3 Using the Elimination Method

Solve the system.

$$-5(2x + 3y = -15) -10x - 15y = 75$$

$$2(5x + 2y = 1) + 10x + 4y = 2$$

$$-1(y = 77)$$

$$5x + 2(-7) = 1$$

$$5x - 14 = 1$$

$$5x = 15$$

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3b) 
$$2x + y = 8$$
  
 $5x - 2y = -16$ 

(8, a)

3c) 
$$6x - 2y = -22$$
  $\left(-3, 2\right)$   $-3x + 4y = 17$ 

$$9x = -2^{-1}$$

$$(6-3)-2y=-2z$$

$$-18-2y=-2z$$

$$+18$$

$$-2y=-4$$

$$y=2$$

## EXAMPLE 5 Solving Special Systems Using the Elimination Method

Solve each system by the elimination method.

$$2(2x + 4y = 5)$$

$$4x + 8y = -9$$

$$-4x - 8y = -10$$

$$\sqrt{x-y}=-10$$
 which  $\sqrt{x-y}=-10$  which  $\sqrt{x-y}=-10$  which  $\sqrt{x-y}=-10$ 

b. 
$$3x - y = 4$$
  
 $-9x + 3y = -12$ 

### 4.4 Applications of Linear Systems

Example 1: A coffee shop sells teas for \$4 each and coffees for \$5 each. If the coffee shop sold 9 drinks for a total of \$40, how many of each type of drink were sold?

a) Write two equations to model this situation.

a) Whenever two equations to mo
$$4(x + y = 9)$$

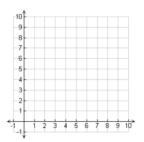
$$4x + 5y = 40$$

this situation.  

$$-4x - 4y = -36$$
  
 $+\frac{4x + 5y}{4} = 40$ 

$$+\frac{4x+5a=40}{4=4}$$

b) Solve the system by graphing.



### **EXAMPLE 2** Solving a Problem about Quantities and Costs

For a production of the musical Wicked at the Ford Center in Chicago, main floor tickets cost \$148, while the best balcony tickets cost \$65. Suppose that the members of a club spent a total of \$2614 for 30 tickets to Wicked. How many tickets of each kind did they buy? (Source: www.ticketmaster.com)

$$-65(x + y = 30)$$

$$148x + 65y = 2616$$

$$X = \#$$
 main floor  $y = \#$  balcony  $y = \#$  ba

$$8 + y = 30$$
  
 $y = 22$ 

8 moun floor, 22 balcony

Example 3:

Jonathan, a second grader, counted the money in his piggy bank. He had only quarters and dimes. When he added up his money, he had 39 coins worth a total of \$7.50. How many coins of each kind did he have?

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$$2 = 40$$
 coins worth a total of \$7.50. How many coins of each kind did he have?

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$$.259 + .1d = 7.5$$
  
 $.159 = 3.6$ 

$$24 + d = 39$$
 $d = 15$ 

24 quarters, 15 dines Example 4:

Lindsey and Gretchen work at two different hair salons and pay different amounts for their station. Lindsey pays \$140 for rent, and \$10 per customer that she works on that month. Gretchen only pays \$100 for rent, but has to pay \$18 per customer. How many customers would it take for them to pay the same amount?

$$100 + 18x = 140 + 10x$$

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#### 4.5 Solving Systems of Linear Inequalities

Date:

Inequality symbols dashed line above Solid line be low

### **EXAMPLE 1** Solving a System of Linear Inequalities

Graph the solution set of the system.

$$\begin{cases} y > -\frac{1}{2}x + 1\\ y \le x + 4 \end{cases}$$

**EXAMPLE 2** Solving a System of Linear Inequalities

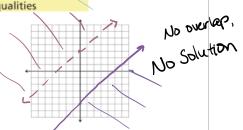


# EXAMPLE 2 Solving a System of Linear Inequalities

Graph the solution set of the system.

$$\begin{cases} y > x + 3 \\ -x + y \le -5 \end{cases}$$

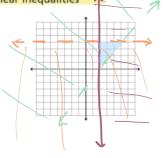
$$( y \le x - 5)$$



# **EXAMPLE 3** Solving a System of Three Linear Inequalities

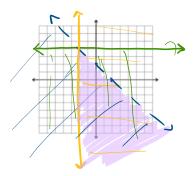
Graph the solution set of the system.

$$\begin{cases} y > \frac{4}{3}x - 3 \\ x \ge 2 \\ y < 4 \end{cases}$$



### Example 4:

$$\begin{cases} x + y < 2 \\ x \ge -2 \\ y \le 4 \end{cases}$$



### Example 5

Write the equations for the system graphed.

